

City University of Hong Kong

Department of Mathematics

MATHEMATICS PLACEMENT TEST FOR MA1200

Sample Questions & Solutions

1. The general solution of the equation $\tan x = 1$ is

A. $x = n\pi + \frac{\pi}{4}$, $n \in \mathbf{Z}$.

B. $x = n\pi \pm \frac{\pi}{4}$, $n \in \mathbf{Z}$.

C. $x = n\pi + (-1)^n \frac{\pi}{4}$, $n \in \mathbf{Z}$.

D. $x = 2n\pi + \frac{\pi}{4}$, $n \in \mathbf{Z}$.

2. The graph of $(y - 2)^2 = 4 - x^2$ is

A. a parabola.

B. a circle.

C. a point.

D. a pair of straight lines.

3. What is the remainder when $1 - x + x^2 - \dots + x^8$ is divided by $x + 1$?

A. -1.

B. 1.

C. 8.

D. 9.

4. Which of the following is an even function of x ?

A. $f(x) = \sin 2x$.

B. $f(x) = |x| \cos 3x$.

C. $f(x) = |x| \tan x$.

D. $f(x) = x^4 - 2x^2 + 1$.

5. $\frac{d^{13}}{dx^{13}}(\sin x) =$

A. $\sin x$.

B. $-\sin x$.

C. $\cos x$.

D. $-\cos x$.

6. Evaluate $\lim_{x \rightarrow 1} \frac{\log_e x}{x^2 - 1}$.

A. 0.

B. $\frac{1}{2}$.

C. 1.

D. -1.

7. Differentiate $\tan^{-1}\left(\frac{1+x^2}{1-x^2}\right)$ with respect to x .

A. $\tan x$.

B. $\frac{1}{1+x^2}$.

C. $\frac{x^2}{1+x^4}$.

D. $\frac{2x}{1+x^4}$.

8. Which of the following is true regarding the function $f(x) = 2x^3 + 3x^2 - 12x + 6$?

A. It has no local maximum point.

B. $x = 0$ is a point of inflexion.

C. It has a local maximum point at $x = 2$.

D. It has a local minimum point at $x = 1$.

Solutions

1. A. $x = n\pi + \frac{\pi}{4}$, $n \in \mathbf{Z}$.

2. B. a circle.

3. D. 9.

4. B. $f(x) = |x| \cos 3x$.

5. C. $\cos x$.

6. B. $\frac{1}{2}$.

7. D. $\frac{2x}{1+x^4}$.

8. D. It has a local minimum point at $x = 1$.